
#### Abstract

Rodrigo Carvalho Winterschool - 30 of January, 2023

The objective of this talk is to discuss a question derived from a construction made in [2]. That is, under which conditions one can construct a regular space with character $\mathfrak{b}$ such that $(X, \tau) \rightarrow(\text { top } \omega+1)_{\omega}^{1}$, and $(X, \tau) \nrightarrow\left(\text { top } \omega^{2}+1\right)_{\omega}^{1}$. An original construction of such space was made in this same paper, using $\diamond$. I will present a construction, made in a joint work with L. Junqueira and G. Fernandes [1], that can be done without $C H$. We also discuss a new development, relating the existence of such spaces with the existence of a Hajnal-Maté graph.


## References

[1] Carvalho, R. Fernandes, G. and Junqueira, L. - Partitions of topological spaces and a new club-like principle, to appear at PAMS, 2023
[2] Komjáth, P. and Weiss, W. - Partitioning topological spaces into countably many pieces, Proceedings of the American Mathematical Society, 101, 4, 767-770, 1987

